



**Prof. Motoko Kotani**  
**Director**  
**Pure mathematician**  
**(Geometer)**

to **Tohoku University and AIMR**

**Susumu Ikeda**

**Associate Professor**  
**Research Support Division (Administrative Director)**

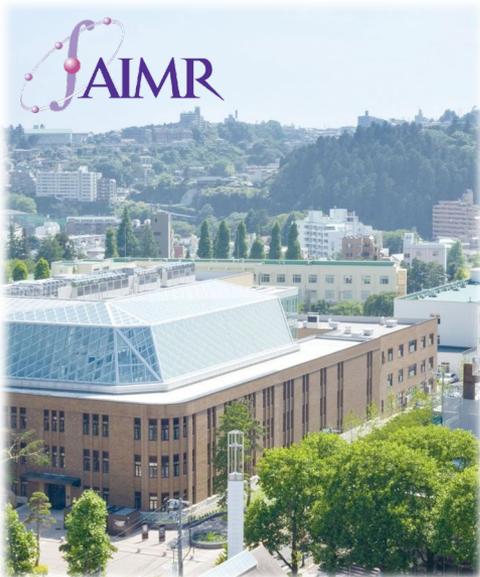
**Institute for Materials Research (WPI-AIMR)**  
**Tohoku University, Japan**

**Minerals Tour**

**Musée de minéralogie MINES ParisTech**  
**Collection of Univ. Pierre et Marie Curie**  
**Muséum national d'Histoire naturelle**

My visits to **France** so far

**1998 Orléans (mineralogy conference), Paris (Quartier Latin)**



Entrance fee: **6 €**

<http://collection-mineraux.sorbonne-universite.fr/fr/index.html>

# 13 WPI Centers

## Sendai City



- Founded in 1907 as the 3<sup>rd</sup> Imperial University in Japan
- “Research First” and “Open-Door” Policy
- The first university which accepted women students, foreign students in Japan

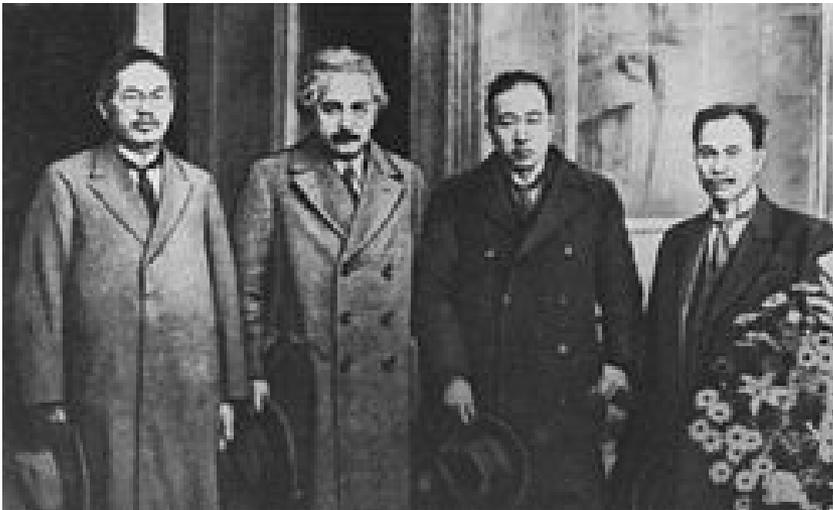


President  
Dr. Hideo OHNO

# Dr. Kotaro HONDA “god of steel”



- 1917 Invention of **KS Steel**, the strongest magnet in the world
- 1916-22 Establishment of *Institute for Materials Research (IMR)*
- 1931-40 President of Tohoku University
- 1937 First recipient of **Order of Culture**, the Japan’s highest cultural honor



With **Albert Einstein** in 1922 at Tohoku Univ.



**KS Steel**

Dr. Honda laid the **foundation of materials science** of not only Tohoku University but also Japan.



## Yagi-Uda Antenna

invented by  
Prof. Shintaro UDA and  
Prof. Hidetsugu YAGI  
in 1926



Invented by

## Prof. Jun-ichi NISHIZAWA 1926-2018



### IEEE Jun-ichi Nishizawa Medal

was established in 2002 in honor of Jun-ichi Nishizawa's  
lifetime of outstanding achievements.

- Light-focusing Glass Fibers (1964)
- Polarization Fibers (1974)
- Avalanche Photodiode (1952)
- PIN Photodiode (1953)
- Semiconductor Lasers (1957)
- Static Induction Thyristor (1970)



# Advanced Institute for Materials Research



# Missions of WPI Research Centers

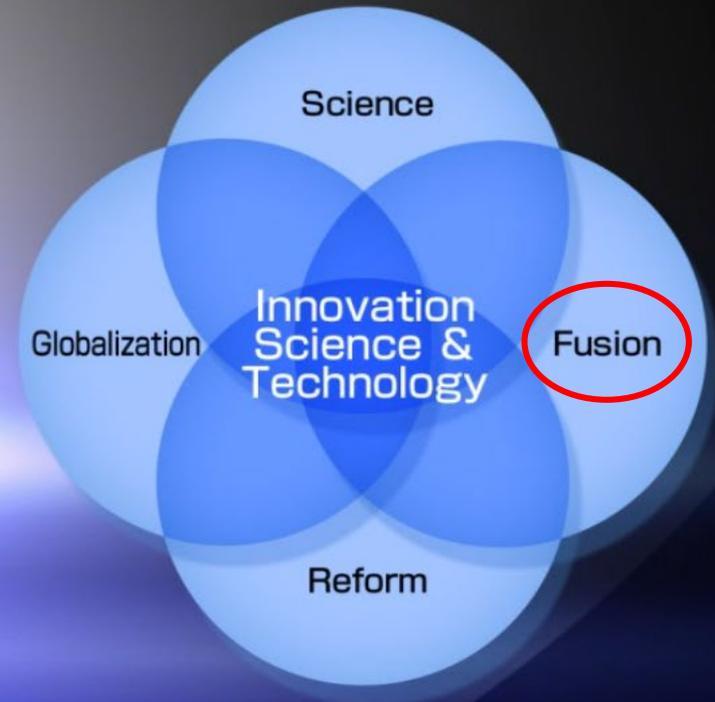
to attract excellent researchers from around the world

**1** Science : Leading-edge research level

**2** Globalization : Realization of an international research environment

**3** Reform : Reform of the research organization

**4** Fusion : Creation of interdisciplinary domains





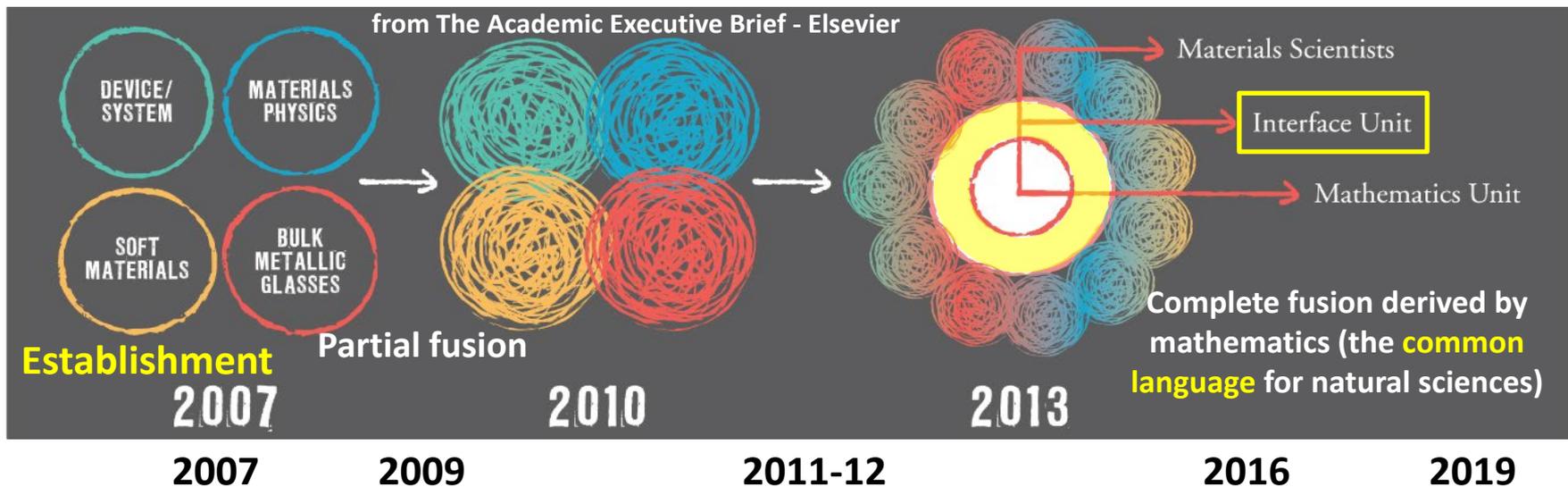
**Motoko Kotani**  
**Director**  
**Pure mathematician**  
**(Geometer)**



**Prof. Kotani** in a photograph taken at the reception held at Rennes City Hall with Deputy Mayor of Rennes (**NanoMat2015**). Our Sendai City is a sister city of Rennes.

## Toward the predictive materials science based on **mathematics-materials science** collaboration

### History of Math-Mate Collaboration at AIMR



~25% of the AIMR researchers are mathematicians or theoretical physicists



Experimental laboratory



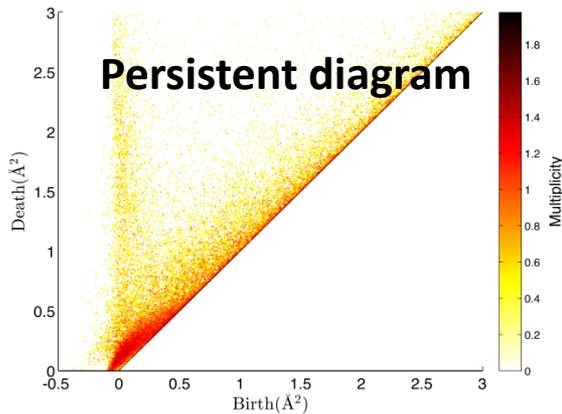
**Math Group**  
WPI-AIMR SINCE 2012



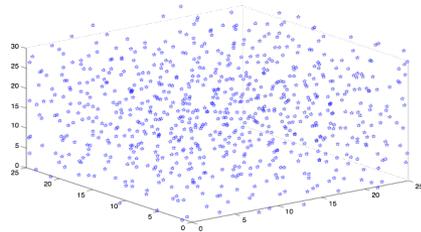
# Structure analysis of amorphous materials

using **persistent homology**

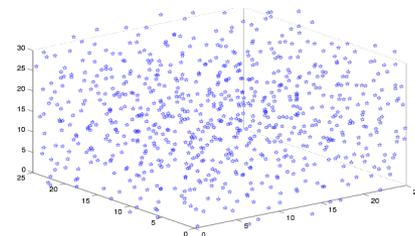
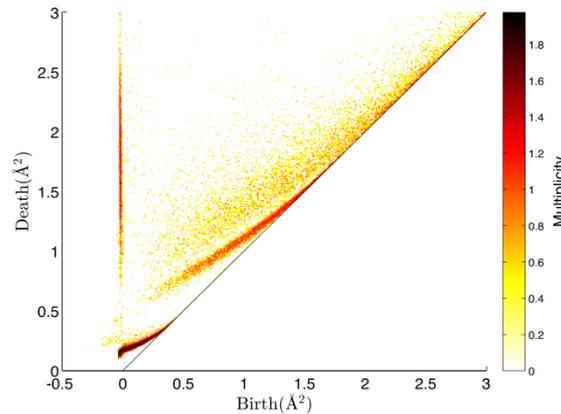
liquid



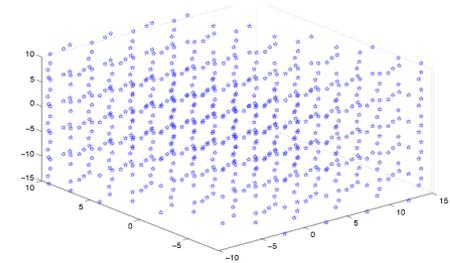
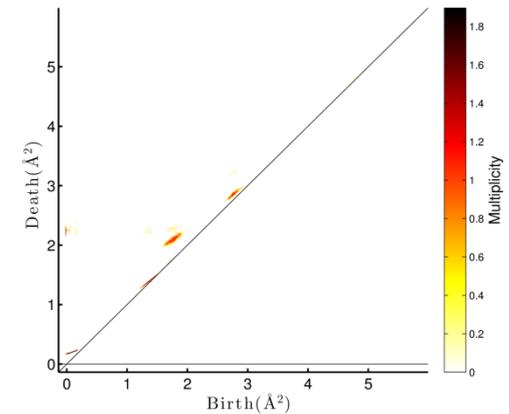
Persistent diagram



amorphous



crystalline



Persistent homology can extract some order hidden in random structures.

Y. Hiraoka, T. Nakamura, A. Hirata, E. G. Escolar, K. Matsue and Y. Nishiura, Hierarchical structures of amorphous solids characterized by persistent homology. *Proceedings of the National Academy of Sciences* **113**, 7035-40 (2016).

T. Nakamura, Y. Hiraoka, A. Hirata, E.G. Escolar and Y. Nishiura, Persistent homology and many-body atomic structure for medium-range order in the glass. *Nanotechnology* **26**, 304001 (2015).

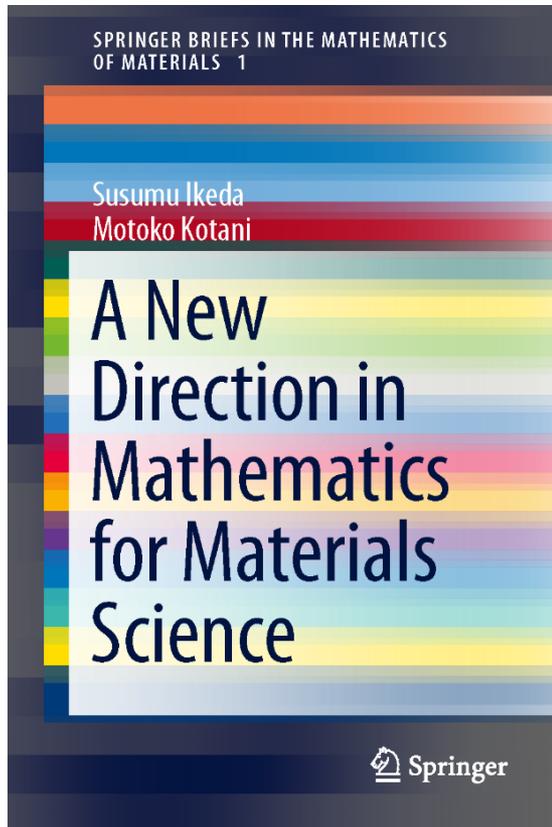


A series of monographs for math-mate collaboration  
“SpringerBriefs in the Mathematics of Materials”

ISSN: 2365-6336

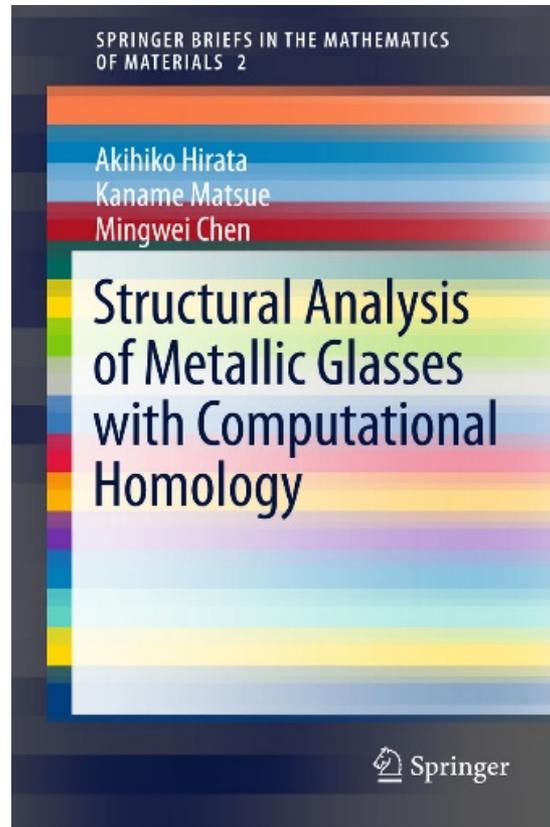
**Editor-in-chief: Motoko Kotani**  
Series Editors: Y. Nishiura, M. Tsukada,  
S.M. Allen, W. Jaeger, S. Luckhaus

**Vol. 1**



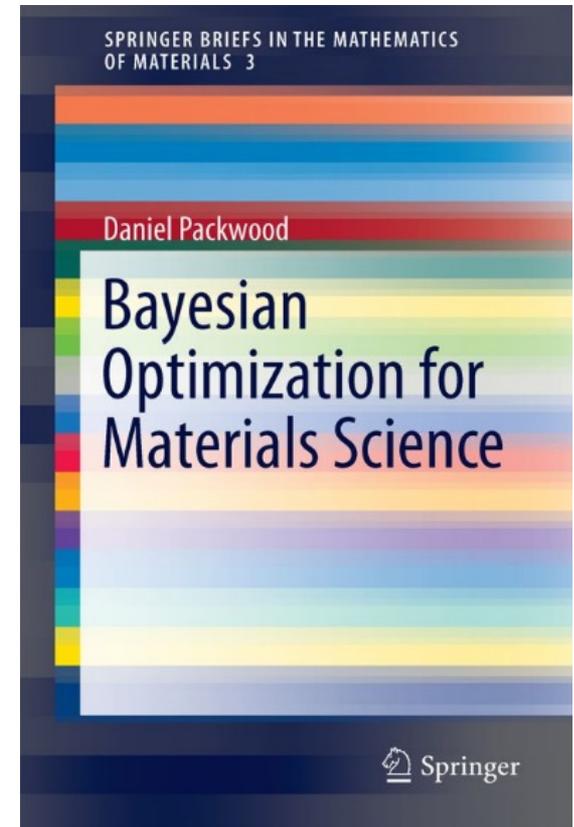
2015

**Vol. 2**



2016

**Vol. 3**



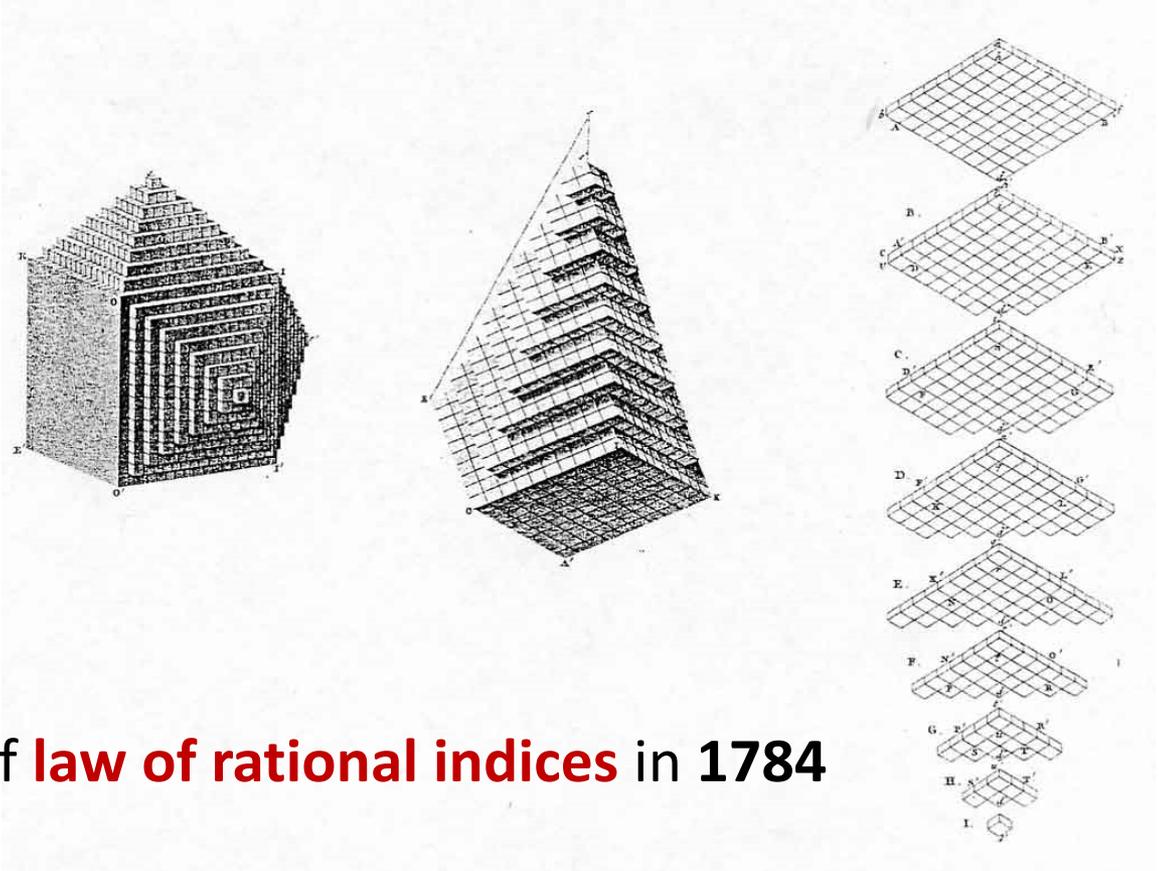
2017

Please refer to these books if you wish to get further information  
about our math-materials collaboration.

# René-Just Haüy (1743–1822)

French mineralogist

*"Father of Modern Crystallography"*



Discovery of **law of rational indices** in **1784**

Materials (crystals) can be expressed based on the mathematical language **"geometry"**.

# Workshop franco-japonais nanomatériaux

**Five researchers are participating in this NanoMat2019 from**



**Advanced Institute for Materials Research,  
Tohoku University**

## **Oral speakers from AIMR at NanoMat2019**



Assoc. Prof. **Hiroshi Yabu**  
Junior Principal Investigator

Nanocomposite materials based on catechol-containing adhesive and reductive polymers



Assoc. Prof. **Akichika Kumatani**

Nanoscale Electrochemical Imaging on Energy Materials: From Lithium-ion (De)intercalation Process to Electrocatalytic Reaction

## **Poster presenters from AIMR at NanoMat2019**



**Dr. Tang Ma**  
Assist. Professor

Functional bio-hybrid membranes through self-assembly



**Dr. Hiroya Abe**  
Assist. Professor

Fe Azaphthalocyanine for Realizing Highly Active Oxygen Reduction Reaction (ORR) Catalytic Electrodes



Assoc. Prof. **Susumu Ikeda**  
Administrative Director

Molecular dynamics simulations of organic semiconductor thin film growth



# Create predictive materials science based on mathematics-materials science collaboration



TOHOKU  
UNIVERSITY

Communication

世界トップレベルの研究者が  
集結するAIMR。  
自由な議論と交流の中から、  
新たな発想は生まれる。

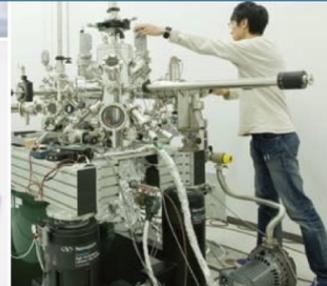
Research  
4つの研究グループと数学ユニット。  
ここには、世界最高水準の研究環境がある。



Thank you for your attention !



材料科学の融合という独創的な取り組みが、材料科学の  
発展にとって分水嶺となったと、いつの日か語られること。

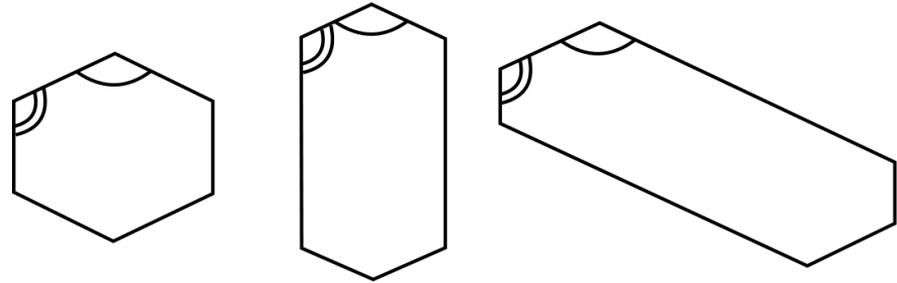


# Nicolas Steno (1638–86)

Danish scientist



Discovery of **law of constant angles** in 1669



First discovery of geometrical characteristics of materials.  
This paved the way for the **Haüy's discovery** in 1784.



Apparatuses to measure an angle which two faces form

# 230 space groups

## Group theory



**Évariste Galois**

(1811–32)



**M. Sophus Lie**

(1842–99)

mathematical means to describe the regularities

- point symmetries
- periodicities (translation symmetries)

## **Proof** of the classification of the **230 space groups** (in 3D)

was independently established by two **mathematicians** and one crystallographer.



mathematician

**E.S. Fedorov**

in 1890



mathematician

**A.M. Schoenflies**

in 1891



crystallographer

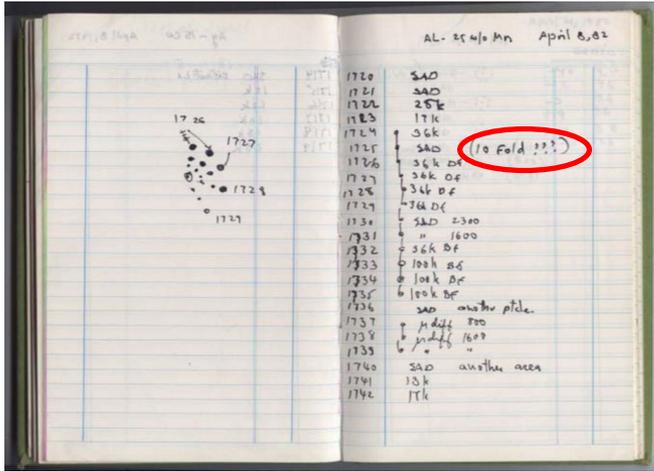
**W. Barlow**

in 1894

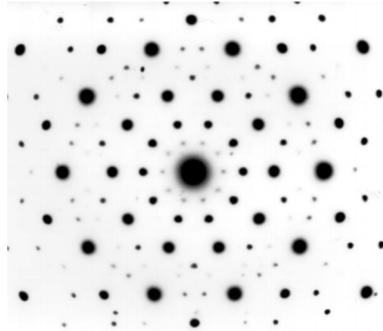
Clearly, **mathematics** is contributing significantly to the development of materials science.

# Quasicrystals

In 1982, Daniel Shechtman observed pentagonal symmetry in the electron diffraction pattern of an aluminum alloy sample.



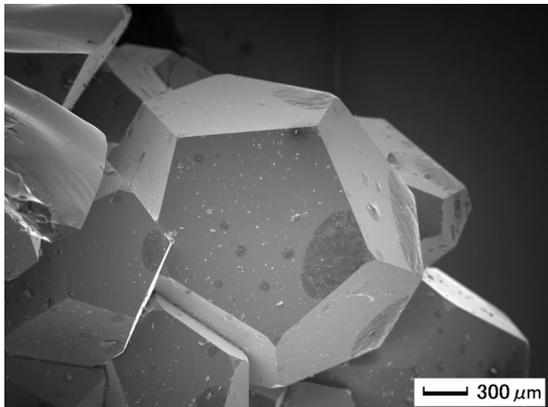
his experimental notebook



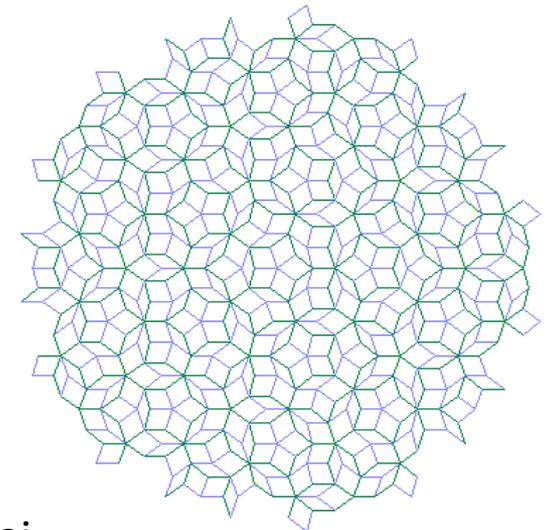
10-fold electron diffraction pattern  
(from Shechtman's presentation file)



Daniel Shechtman  
(Lecture at Tohoku University)



Zn-Mg-Dy quasicrystals,  
courtesy of the late Prof. An-Pang Tsai,  
Tohoku University



**Penrose tiling**  
(Wikimedia Commons)

1600

1700

1800

1900

2000

2100

# Materials science

Earthenware  
Metal ware

Mineralogy

Crystallography

Metallurgy

Ceramics

Surface Science

Semiconductor

Device engineering

Solid State Physics

Spintronics



1669



Symmetry

Bartholinus

Law of constant angle

Double refraction  
(Birefringence)



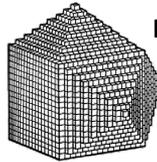
Optics



Periodicity

Haüy

Law of rational indices



Space Group

Group Theory



Galois



Lie

Eigenvalue problem

$$|A - \lambda E| = 0$$

Linear Algebra

$$(\tilde{A}WA)_x = \tilde{A}W_y$$



Euler



Gauss

Modern Geometry

$$e^{i\theta} = \cos \theta + i \sin \theta$$

Wave of electrons

Bloch's theorem



$$\psi_{\vec{k}}(\vec{r}) = e^{i\vec{k} \cdot \vec{r}} u_{\vec{k}}(\vec{r})$$



Quantum mechanics

$$Hx = \epsilon x$$

Electronic properties



Kohn

Density functional theory (DFT)

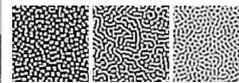
$$\rho(\mathbf{r}) = \sum_i |\phi_i(\mathbf{r})|^2$$

Self organization



Turing

Pattern formation

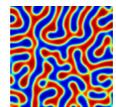


$$\frac{\partial u}{\partial t} = f(u, v) + D_u \Delta u$$
$$\frac{\partial v}{\partial t} = g(u, v) + D_v \Delta v$$

Prigogine



Phase separation

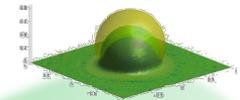


Cahn

Allen-Cahn equation

Cahn-Hilliard equation

$$\frac{\partial c}{\partial t} = D \nabla^2 (c^3 - c - \gamma \nabla^2 c)$$



Level set methods



Osher

Advanced numerical techniques

Noncommutative geometry

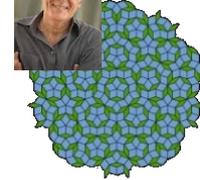


Connes

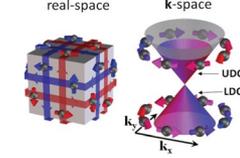
Advanced Geometry



Shechtman



Quasi crystals



Topological insulator

# Mathematics



Euclidean Geometry

Infinitesimal calculus

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$



Newton

Leibniz



# Research groups

Materials Physics  
 Soft Materials  
 Non-equilibrium Materials  
 Device / System  
 Mathematical Science

## Management

Director : **M. Kotani**  
 Deputy Director : **S. Orimo**  
 Adm. Director: **S. Ikeda**  
 Deputy Adm. Director : **M. Funada**

## Executive Advisor

Masaru Tsukada  
 Yasumasa Nishiura

## International Advisory Board

**J.G. Bednorz**, IBM Zurich  
 1987 Physics Nobel laureate  
**H. Gleiter**, Karlsruhe Inst. Tech.  
**V. Narayanamurti**, Harvard Univ.  
**E. Negishi**, Purdue Univ.  
 2010 Chemistry Nobel laureate  
**S. Mori**, Kyoto Univ.  
 1990 Fields Medalist



**M. Kotani**  
 (Institute Director)

**G Leader**




**S. Orimo** (AIMR)      **S. Mizukami** (AIMR)




**S. Samukawa** (AIMR)      **S. Fukami** (AIMR)

**Device/System**



**H. Yabu**  
 (AIMR)

**G Leader**







**K. Tanigaki** (AIMR)      **T. Fukumura** (AIMR)      **T. Sato** (AIMR)      **Y. Ikuhara** (U Tokyo)      **E. Saitoh** (U Tokyo)

**Materials Physics**






**Y.P. Chen** (Purdue U)      **T. Dietl** (Polish Acad Sci)      **A.L. Shluger** (UCL)      **Q.-K. Xue** (Tsinghua U)

**G Leader**

**Mathematical Science**




**H. Suito** (AIMR)      **M. Kotani** (AIMR)




**H. Chiba** (AIMR)      **C. Pickard** (U Cambridge)

**G Leader**

**Nonequilibrium Materials**



**M.W. Chen**  
 (Johns Hopkins U)



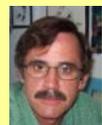

**D. Louzguine** (AIMR)      **A.L. Greer** (U Cambridge)

**G Leader**




**T. Adschiri** (AIMR)      **M. Yamashita** (AIMR)

**Soft Materials**

**A. Hirano** (AIMR)      **T.P. Russell** (UMass Amherst)

# Origins of Universe/ Earth - Life/ Intelligence

*Origin of Earth and Life*

**13**  
**WPI**  
**Centers**



Tokyo Tech 2012



U. Tokyo 2007  
*Origin of Universe*

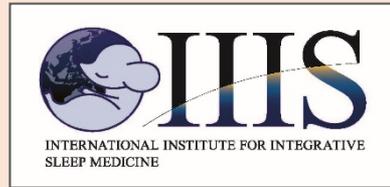
# Life Science

*Immunology*



Osaka U. 2007

*Sleep*

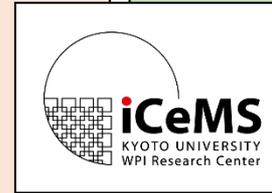


U. Tsukuba 2012

**ASHBi**

Kyoto U. 2018  
*Human biology*

*Cell biology & materials*



Kyoto U. 2007



Nagoya U. 2012

*Plant biology & chemistry*



Kanazawa U. 2017

*Nano life science*

# Materials/ Energy

*Materials & mathematics*



Tohoku U. 2007

*Nanoarchitectonics*



NIMS 2007

*Energy*



Kyushu U. 2010



Hokkaido U. 2018  
*chemistry*

*Origin of Intelligence*



U. Tokyo 2017

# Data/Information Science